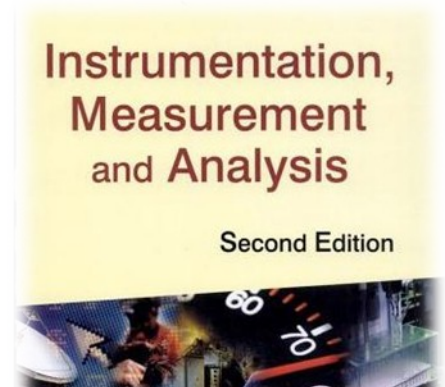


# US06CPHY06

## Instrumentation and Sensors

### UNIT 2 Part 2

## Pressure Measurements



#### UNIT- II Transducer Elements, Pressure Measurements

**Transducer Elements:** Ionization Transducers, Mechno-Electronic Transducer, Opto-Electrical Transducer, Photo-emissive Transducer, Photo-conductive Transducer, Photo-voltaic Transducer

**Pressure Measurements:** Introduction, Moderate Pressure Measurements, Manometers, High Pressure Measurements, Low Pressure (Vacuum) measurements, McLeod Gauge, Thermal conductivity or Pirani Gauge, Ionization Gauge, Knudsen Gauge

# Pressure Measurements

## What is 'Pressure' ?

**Pressure: Force exerted by a fluid on unit surface area of a container i.e.  $P = F/A$ .**

### Units

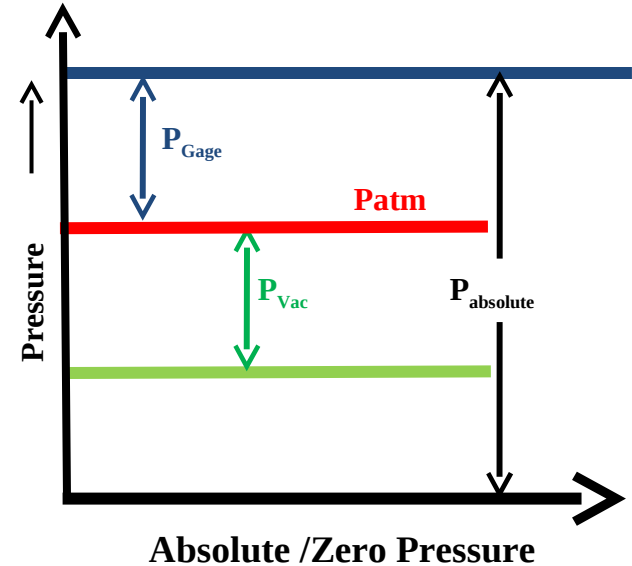
- $\text{N/m}^2 = \text{Pascal (Pa)}$
- $\text{lb/in}^2 = \text{psi}$
- atm
- mm of Hg
- Torr

At sea level pressure is of:

$1 \text{ atm} = 760 \text{ mm of Hg}$   
 $= 760 \text{ Torr}$   
 $= 1.013 \times 10^5 \text{ Pa}$   
 $= 14.7 \text{ psi}$

### Types

- Static
- Dynamic
- Gage
- Absolute
- Vacuum



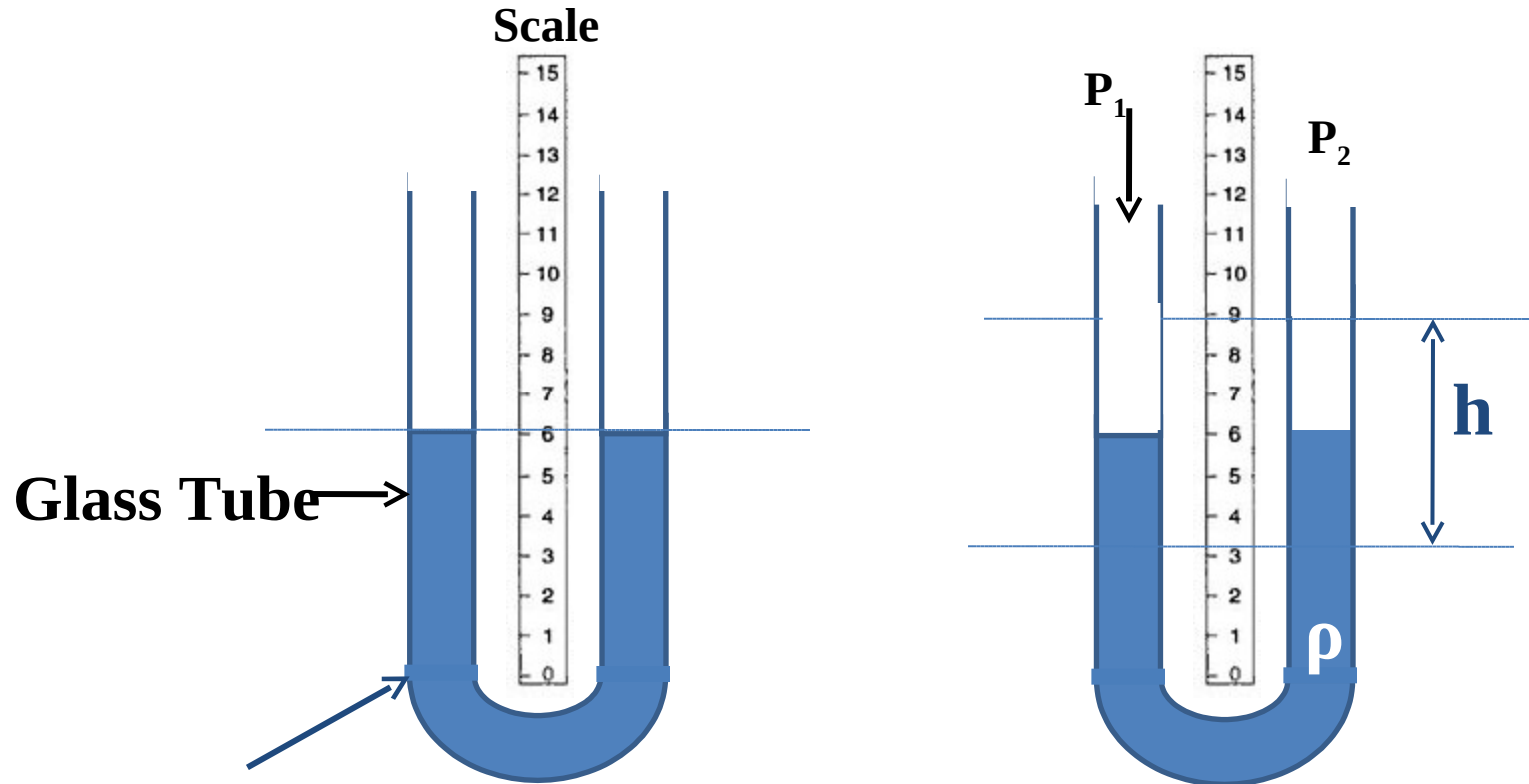
## Pressure Measurement : Range & Techniques

- **Very High** > 1000 atm
- **Moderate**
- **Very Low** < 1mm of Hg (Torr)

Static OR Dynamic e.g. compressors of engine.

- Moderate Pressure Measurements: Manometers : **Static Pressure**
- Other devices using **elastic elements**: For both **Static and Dynamic Pressure**

### Manometers: **Static Pressure** Measurements



Mercury/Water/Fluid

$$P_1 - P_2 = h \rho g$$

If  $P_2$  is  $P_{atm}$  then,  $(P_1 - P_2)$  gives gage pressure (applied).

# Manometers:

## Manometer fluid Characteristics

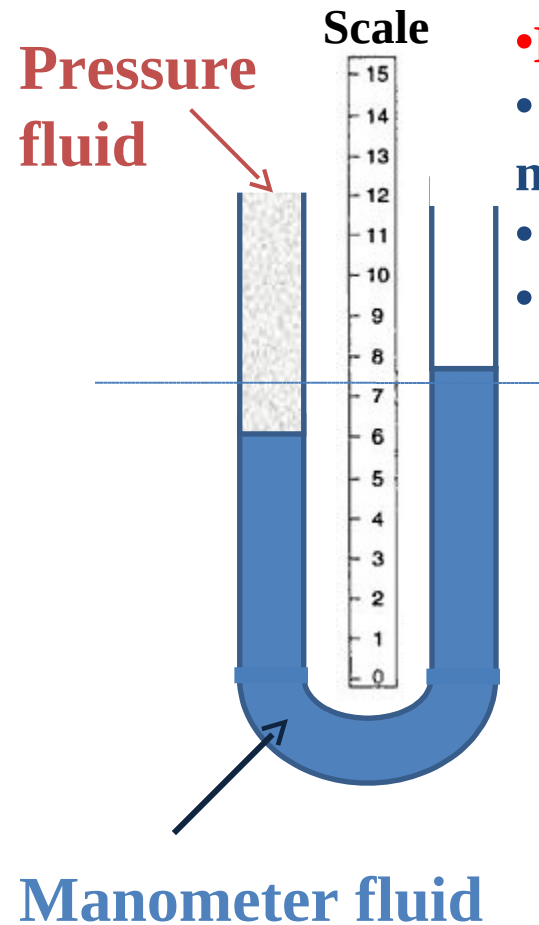
- **Non-Corrosive**
- **No chemical reaction with fluid** whose pressure is to be measured
- **Low viscosity** for quick adjustment with pressure change
- **Negligible surface tension and capillary effects**

## Why manometers are modified ?

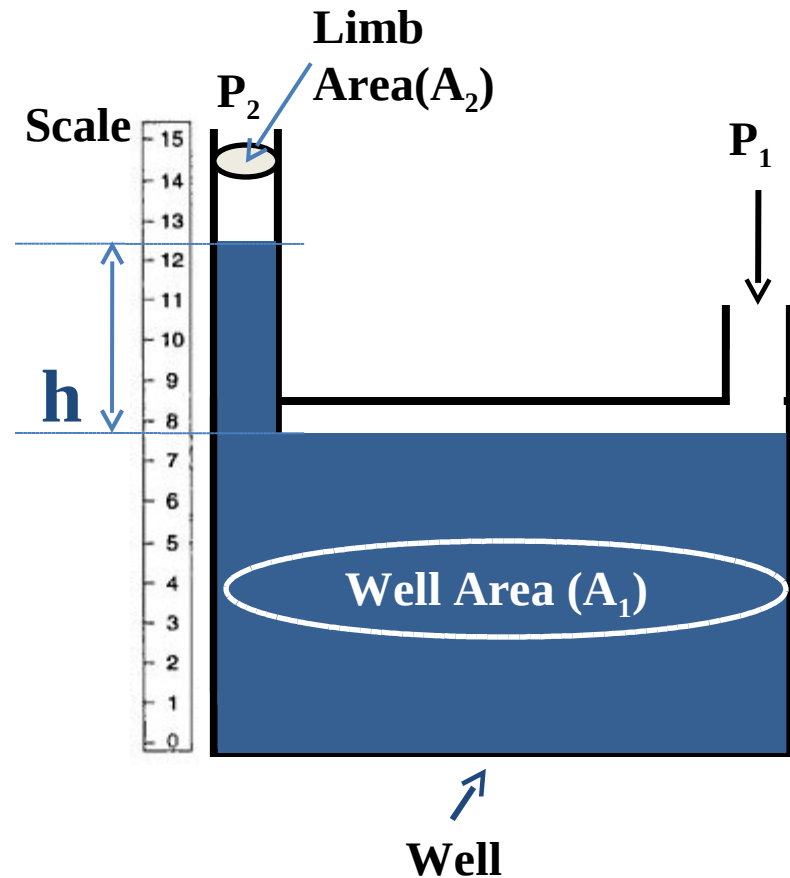
- **For ease in use**
- **To increase sensitivity**

## Types of Modified Manometers

- Cistern or Well Type
- Inclined Tube Type
- Movable Tube Type
- Micrometer Type
- Micro manometer with motor drive and digital read out.



# Cistern or Well type Manometer



Since  $A_1 \gg A_2$ ,

**Change in limb level**  $\gg$

**Change in well level**

So, Change in well level is **ignored** and reading of only one limb (h) is recorded.

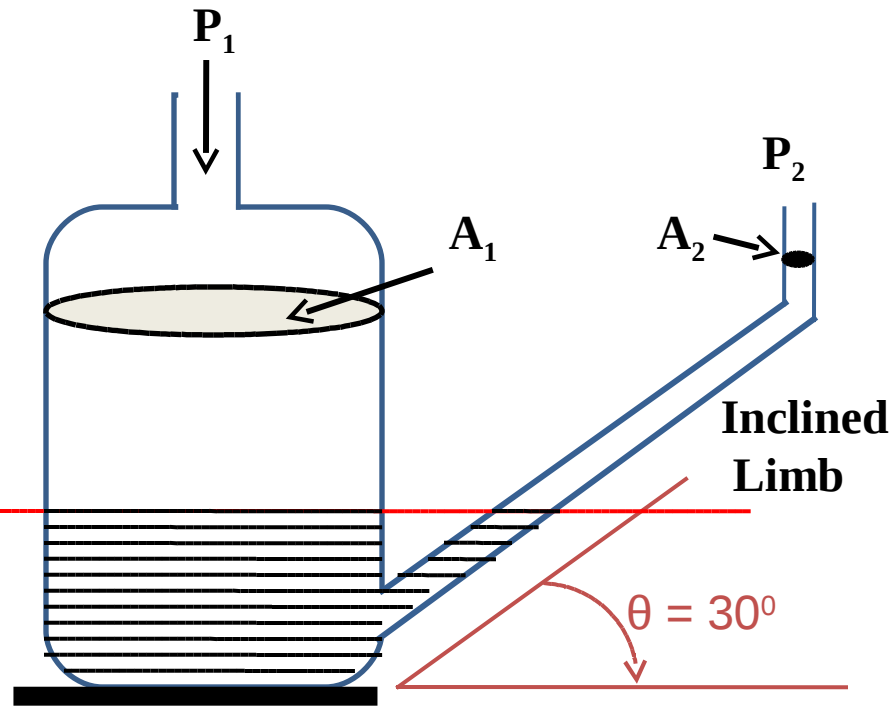
If  $P_1$  and  $P_2$  are absolute pressure, then force equilibrium gives

$$P_1 A - P_2 A = A h \rho g \quad (\text{since } P = F/A)$$

$$\text{i.e. } P_1 - P_2 = h \rho g$$

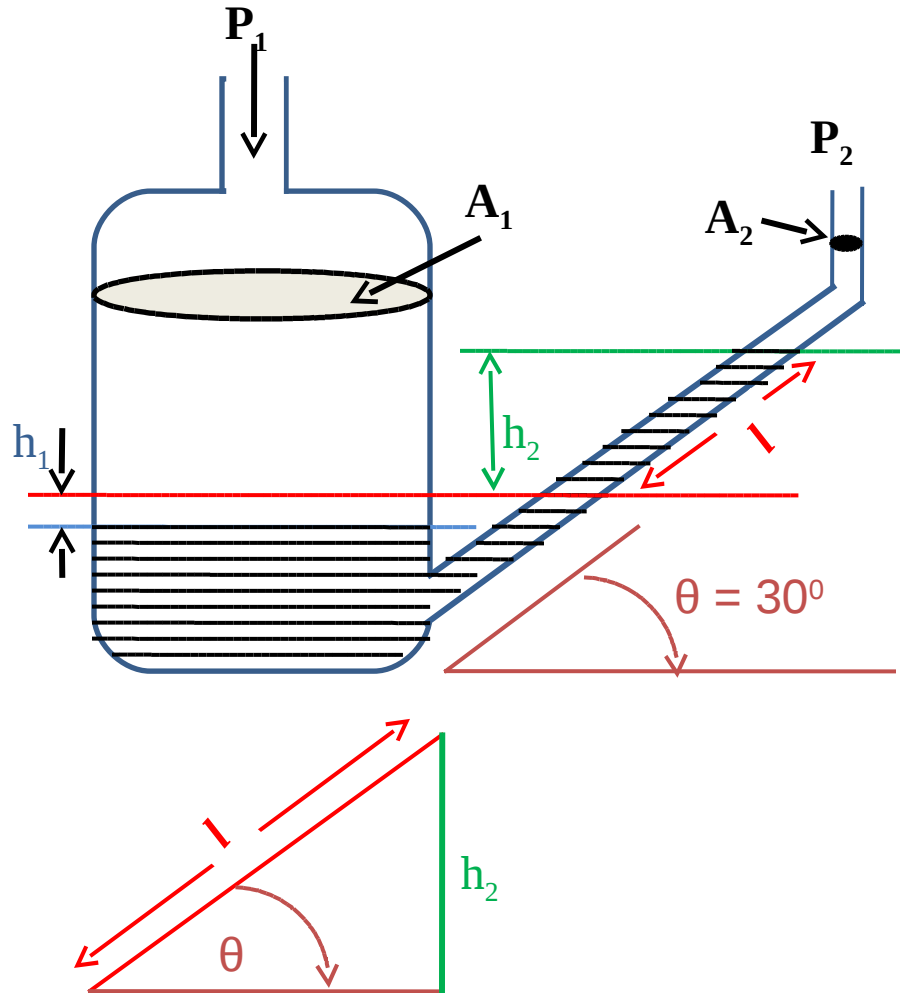
If  $P_2$  is  $P_{atm}$  then,  $(P_1 - P_2)$  gives Gage pressure (applied).

# Inclined Tube Manometer



**When  $P_1 = P_2$   
i.e. equilibrium**

# Inclined Tube Manometer



$$(h_1 + h_2) \rho g = P_1 - P_2 \quad \dots (1)$$

$$\therefore h_1 + h_2 = \frac{P_1 - P_2}{\rho g} \quad \dots (2)$$

Also,  $A_1 h_1 = A_2 l$

$$\therefore h_1 = \frac{A_2}{A_1} l \quad \dots (3)$$

From the geometry of the system,

$$\sin \theta = \frac{h_2}{l} \quad \therefore h_2 = l \sin \theta \quad \dots (4)$$

Using (3) & (4) in (1)

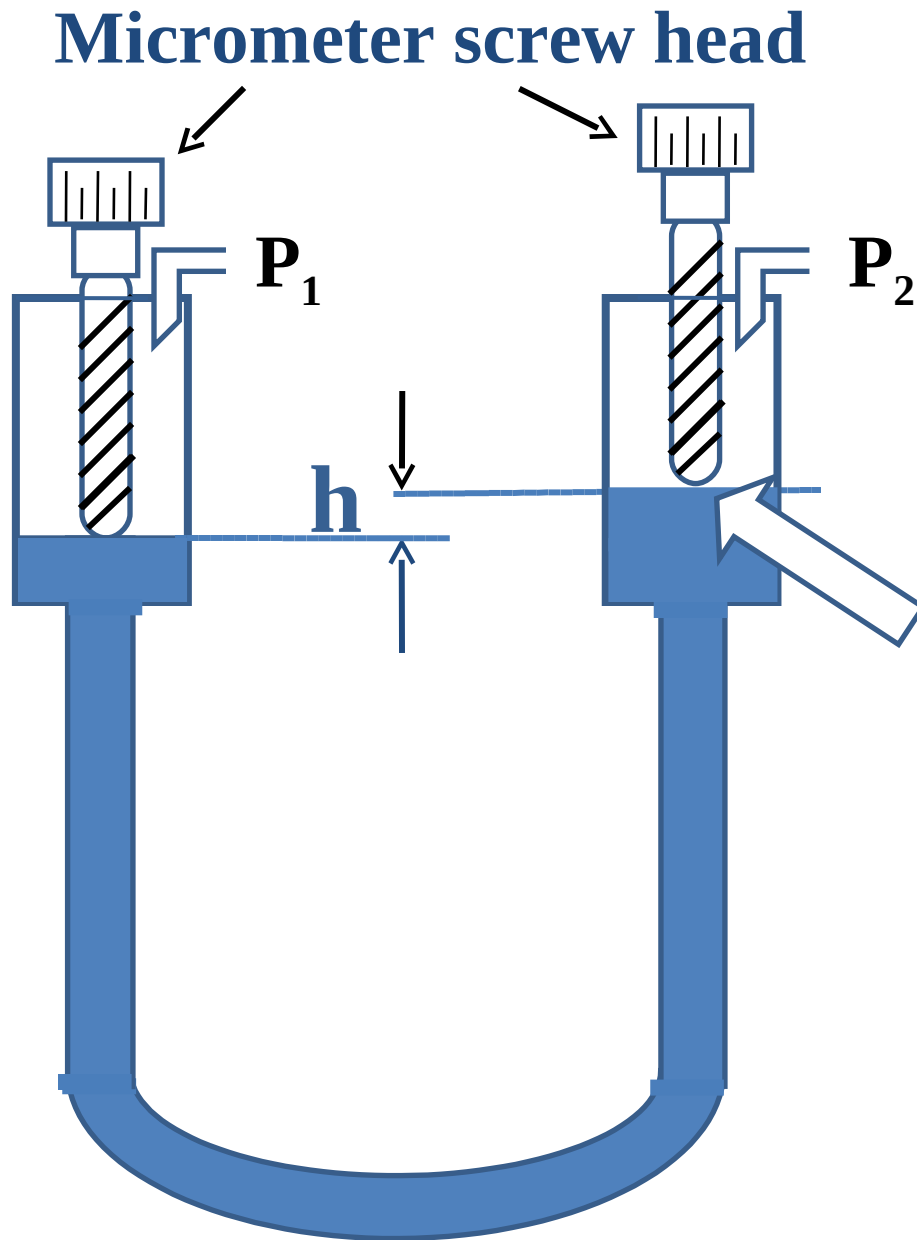
$$\therefore P_1 - P_2 = \left( \frac{A_2}{A_1} l + l \sin \theta \right) \rho g$$

$$\therefore P_1 - P_2 = \left( \frac{A_2}{A_1} + \sin \theta \right) l \rho g$$

Since  $A_1 \gg A_2$ ,  $P_1 - P_2 = \rho g l \sin \theta = \rho g h_2$

if  $\theta = 30^\circ$  then,  $h_2 = l \sin \theta = \frac{l}{2}$  and so  $l = 2h_2$

# Micrometer Type Manometer

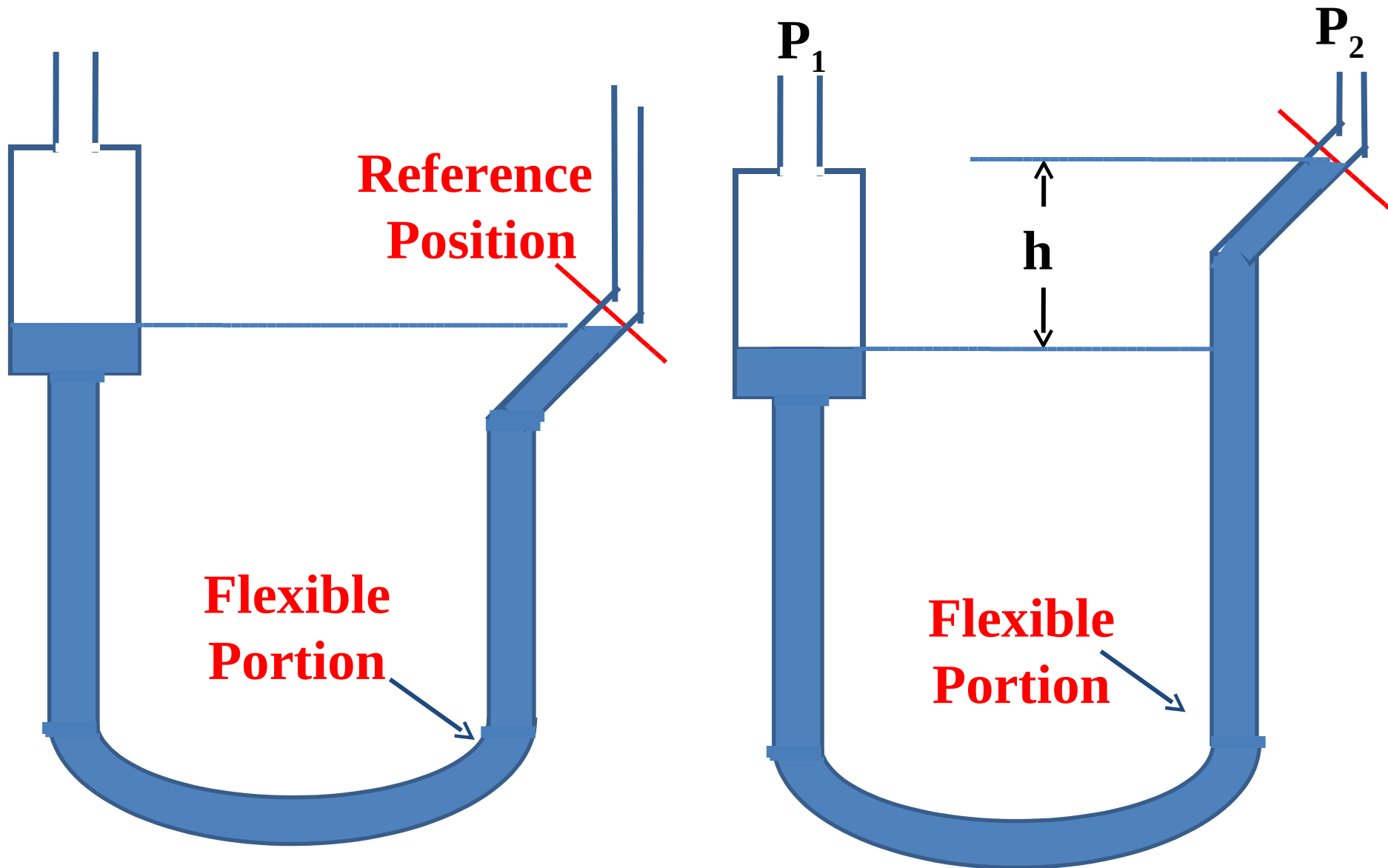


➤ Increased accuracy in reading of the output of manometer i.e. **liquid displacement**.

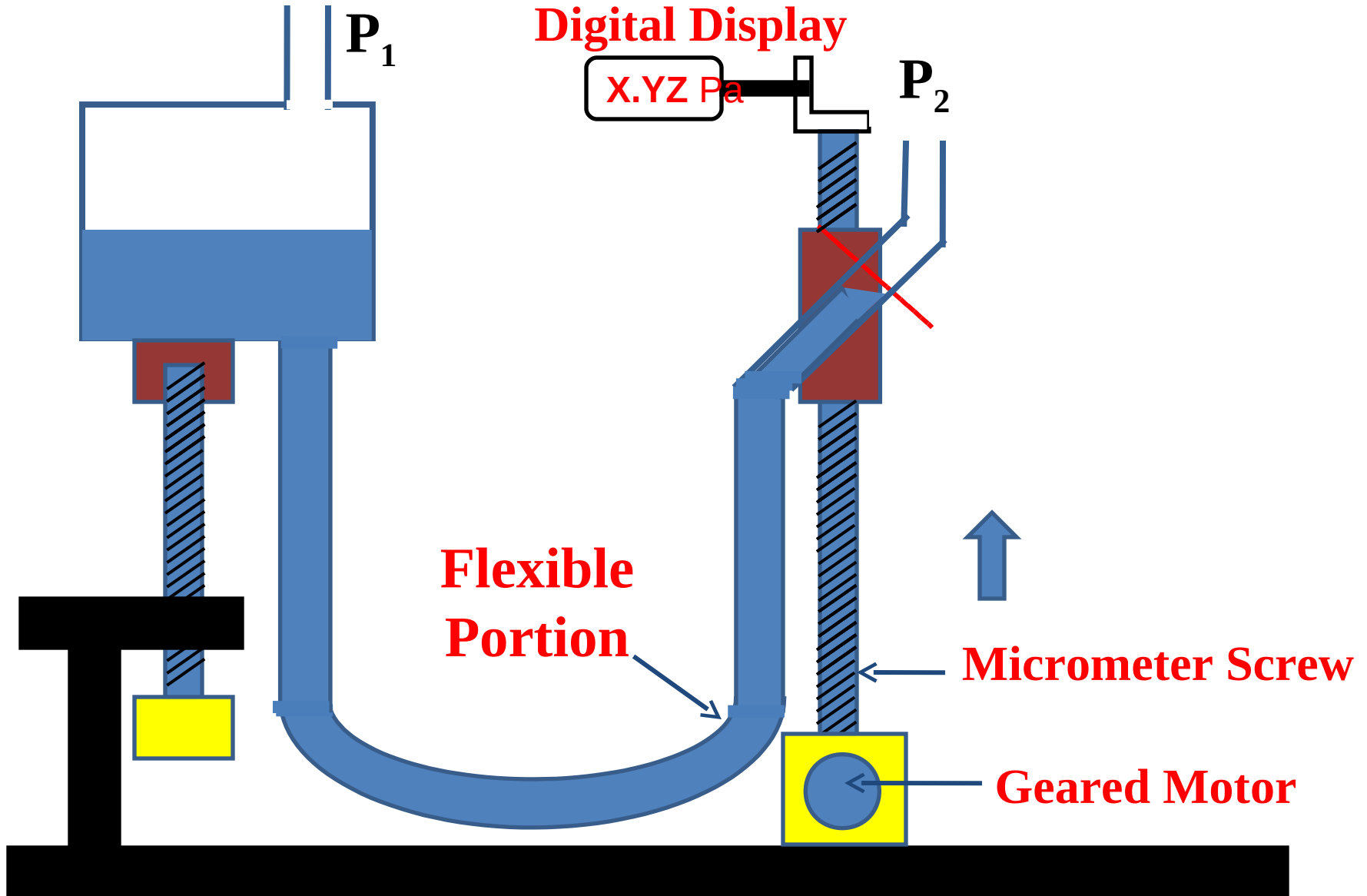
➤ Contact between **micrometer screw** and **liquid level** can be sensed electrically for more accuracy



# Movable Tube Type Manometer

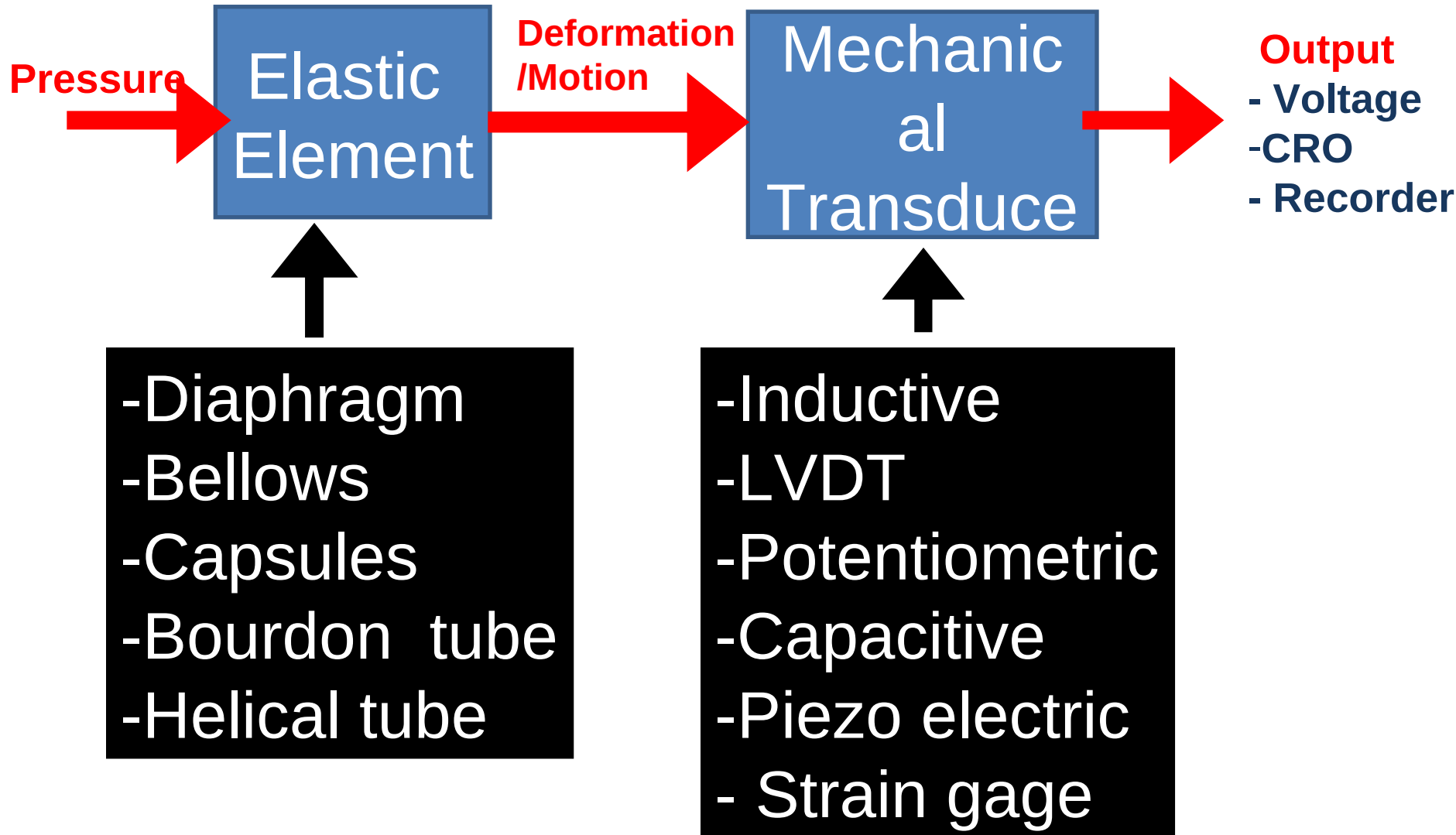


# Micrometer with motor-drive Type Manometer

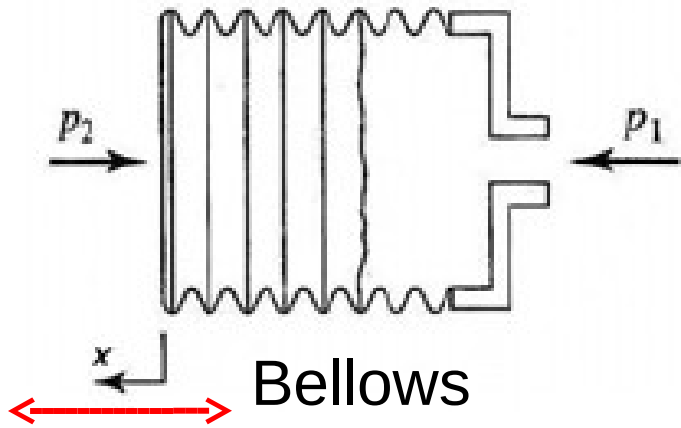


# Elastic Transducers: Static/Dynamic Pressure

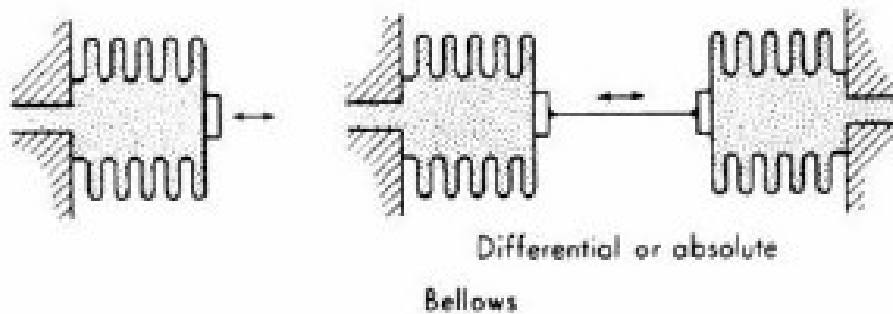
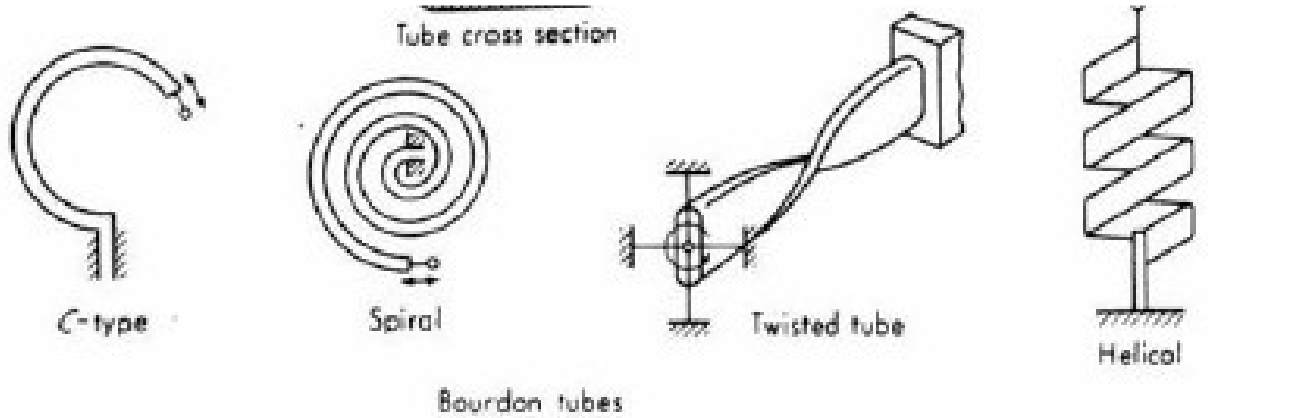
## Principle of Working:



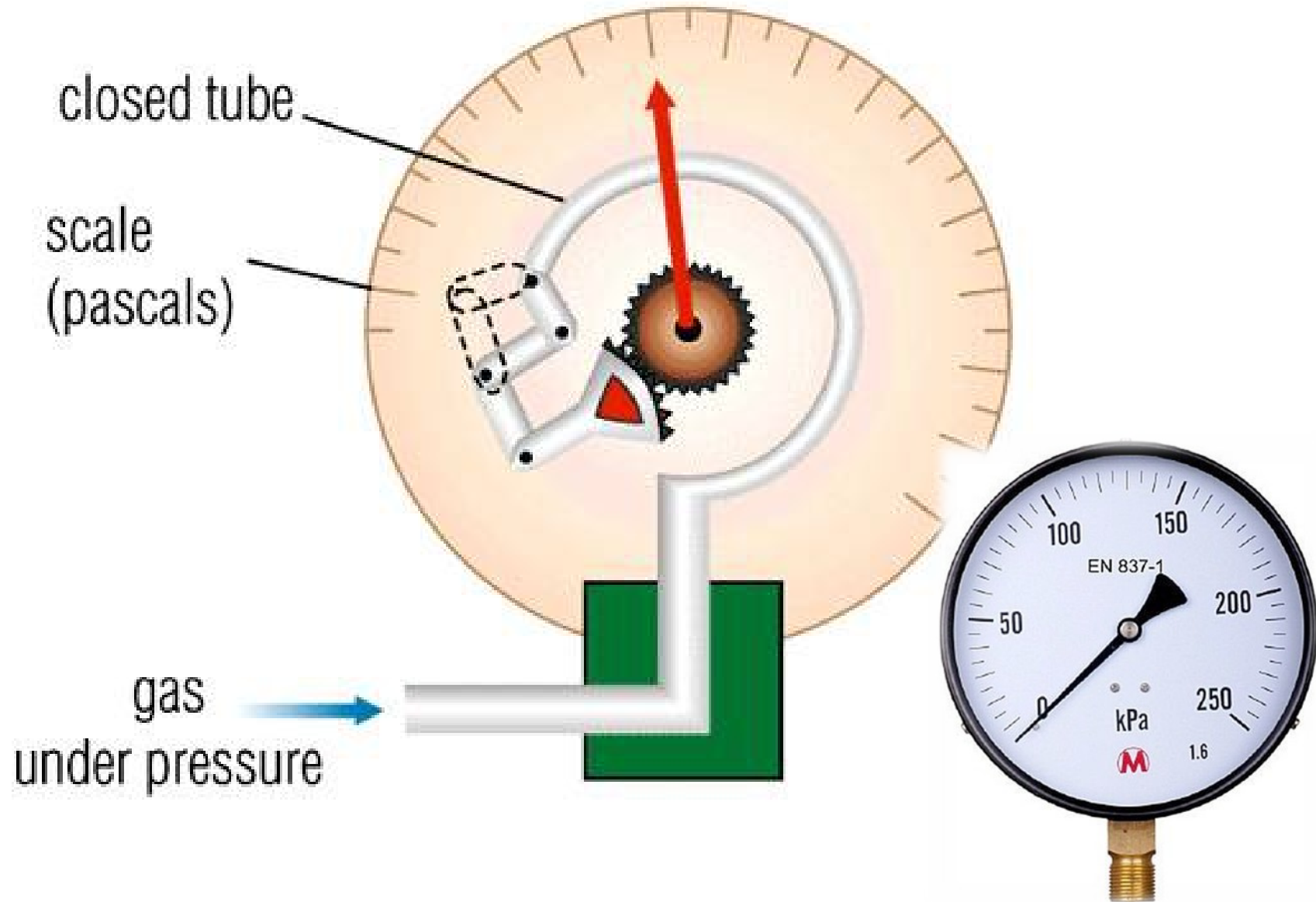
# Elastic Elements:



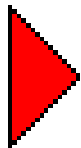
# Elastic Elements:



# Bourdon Gage:



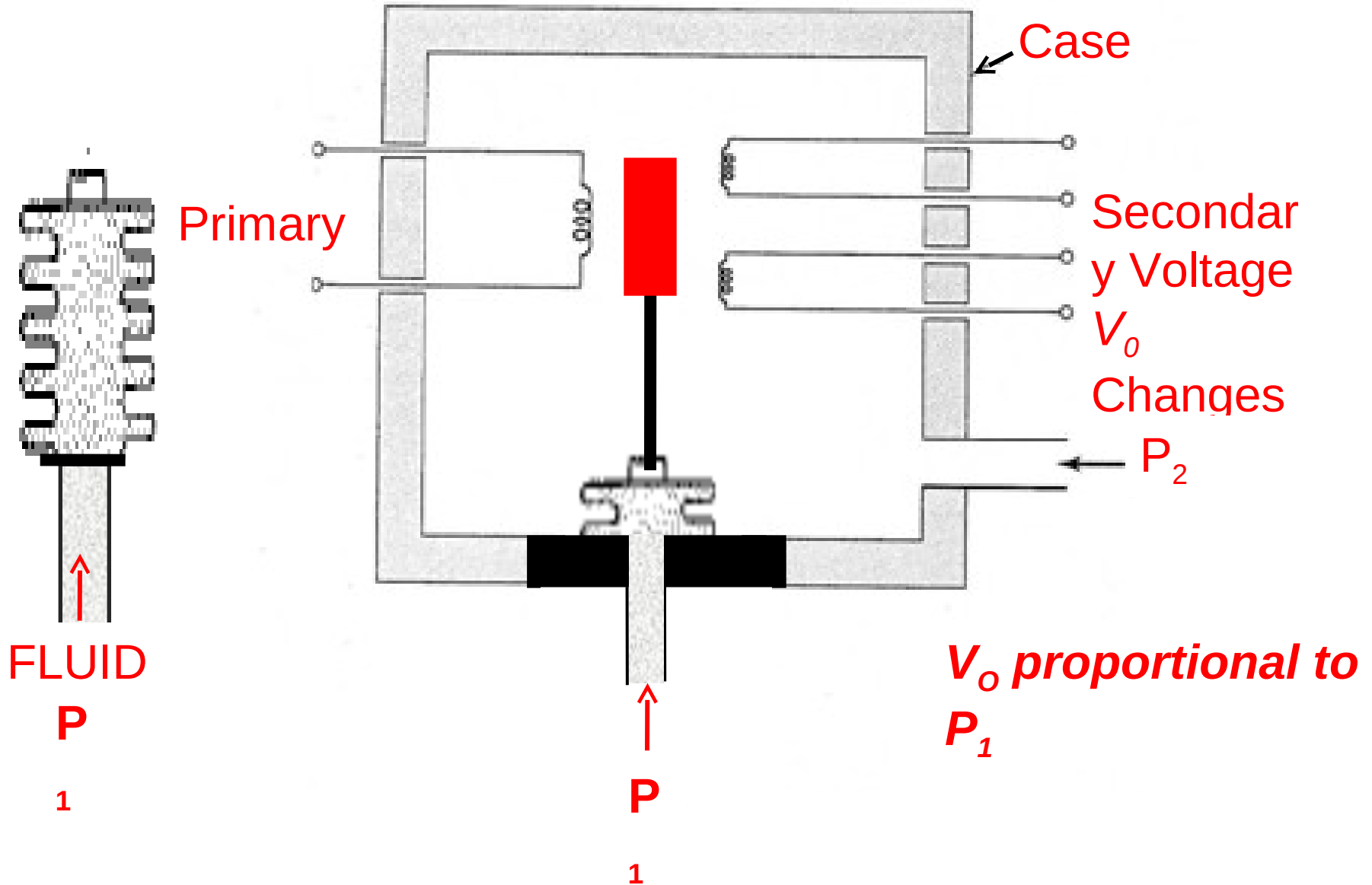
# Bourdon Gage:



## Bourdon Tube Gauge

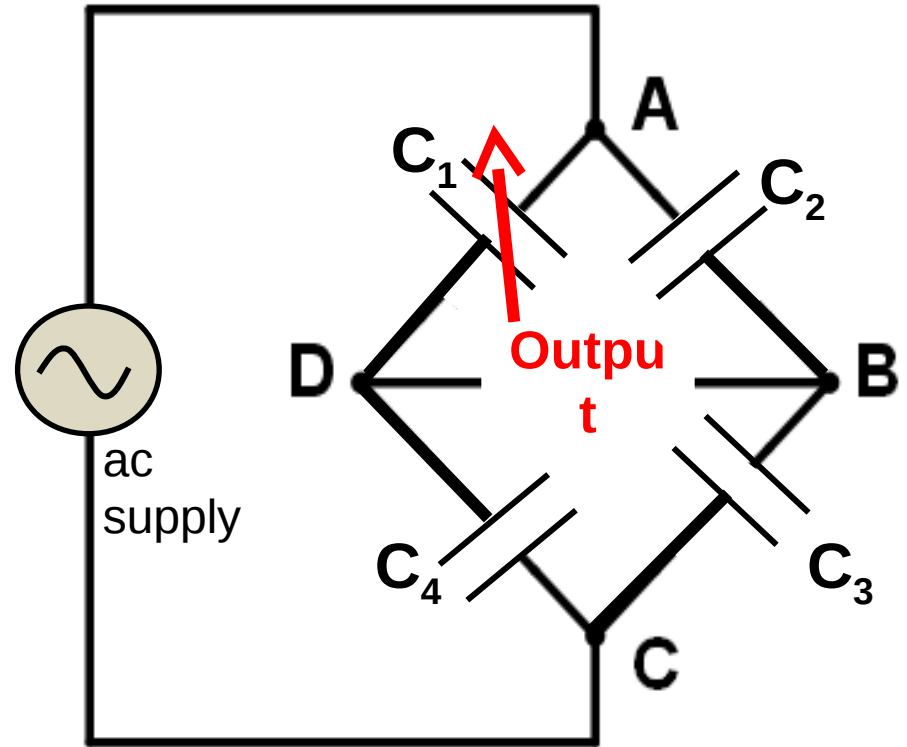
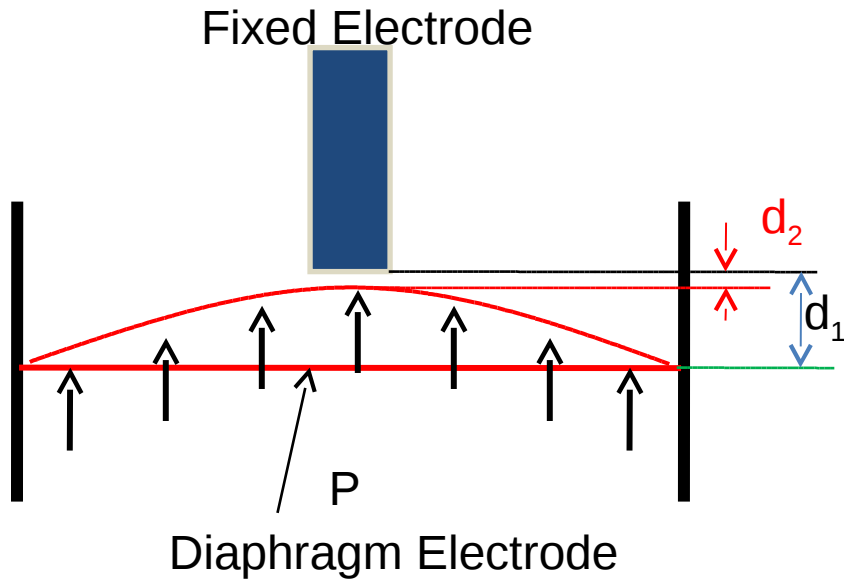
© 2002-2009 Massaya Advanced Technology Education Center

# LVDT Type Pressure Transducer



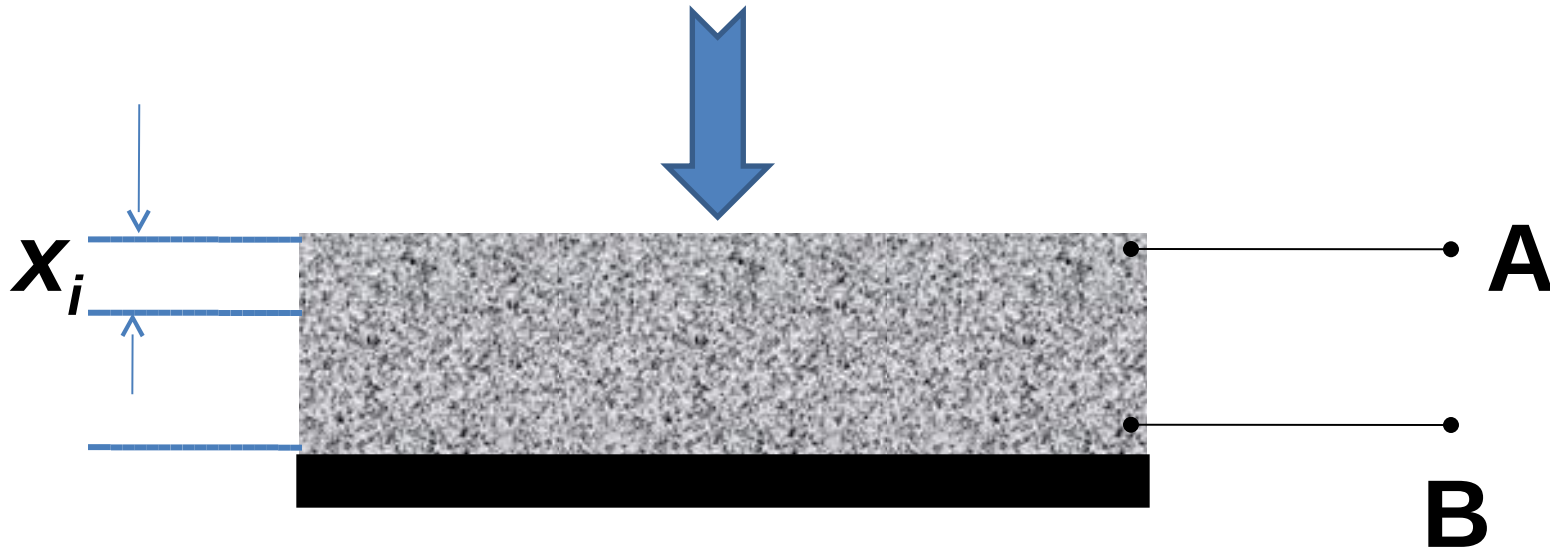


# Variable capacitance Type Pressure Transducer



**Due to pressure diaphragm displaces and Capacitance changes**

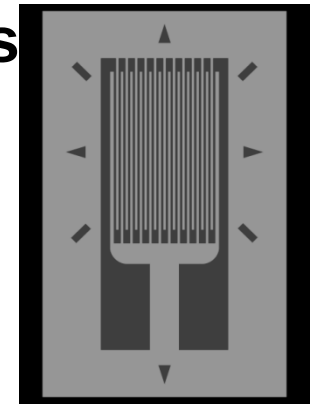
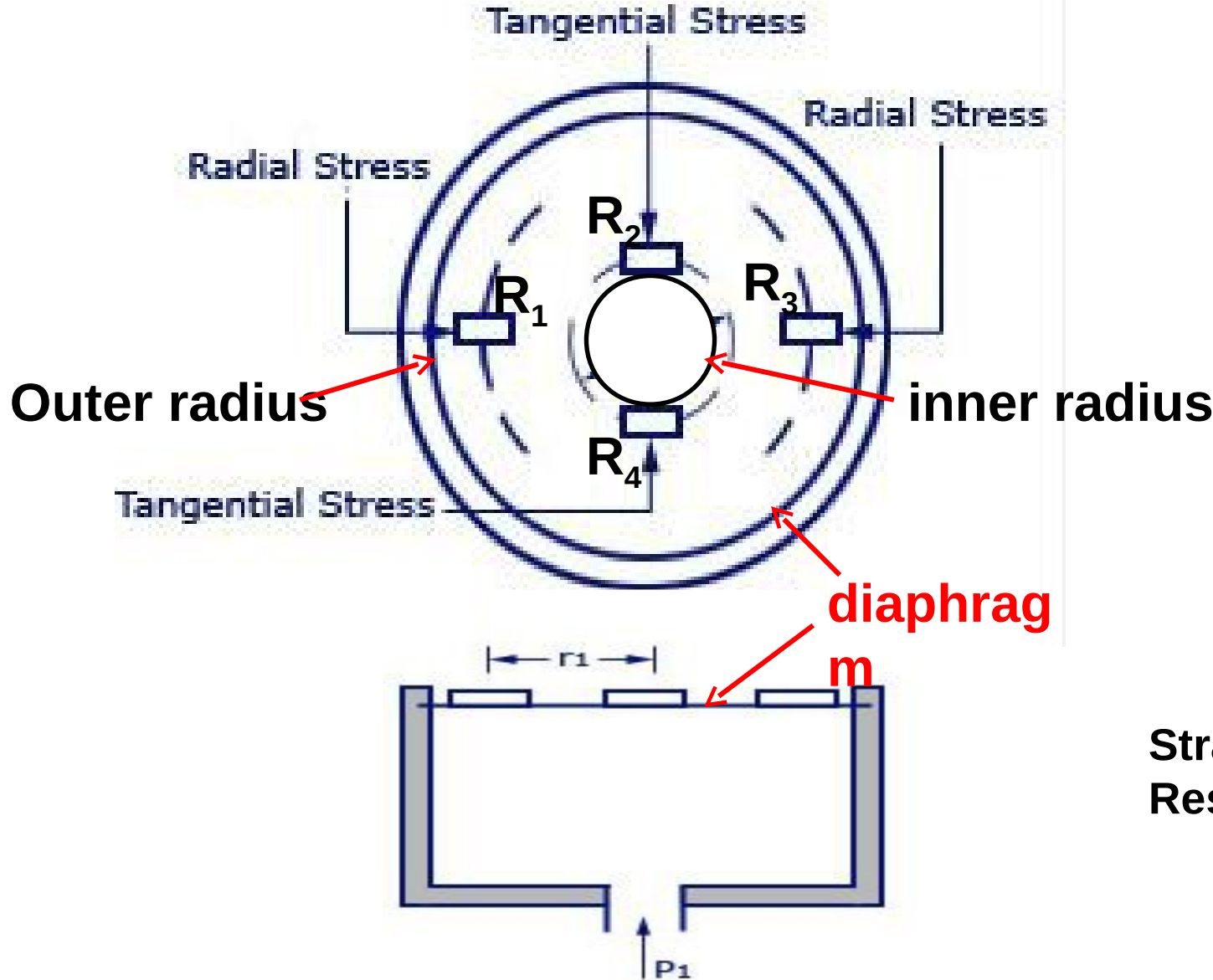
# Piezo-electric Type Pressure Transducer



Due to pressure crystal squeezes to produce voltage between A and B .

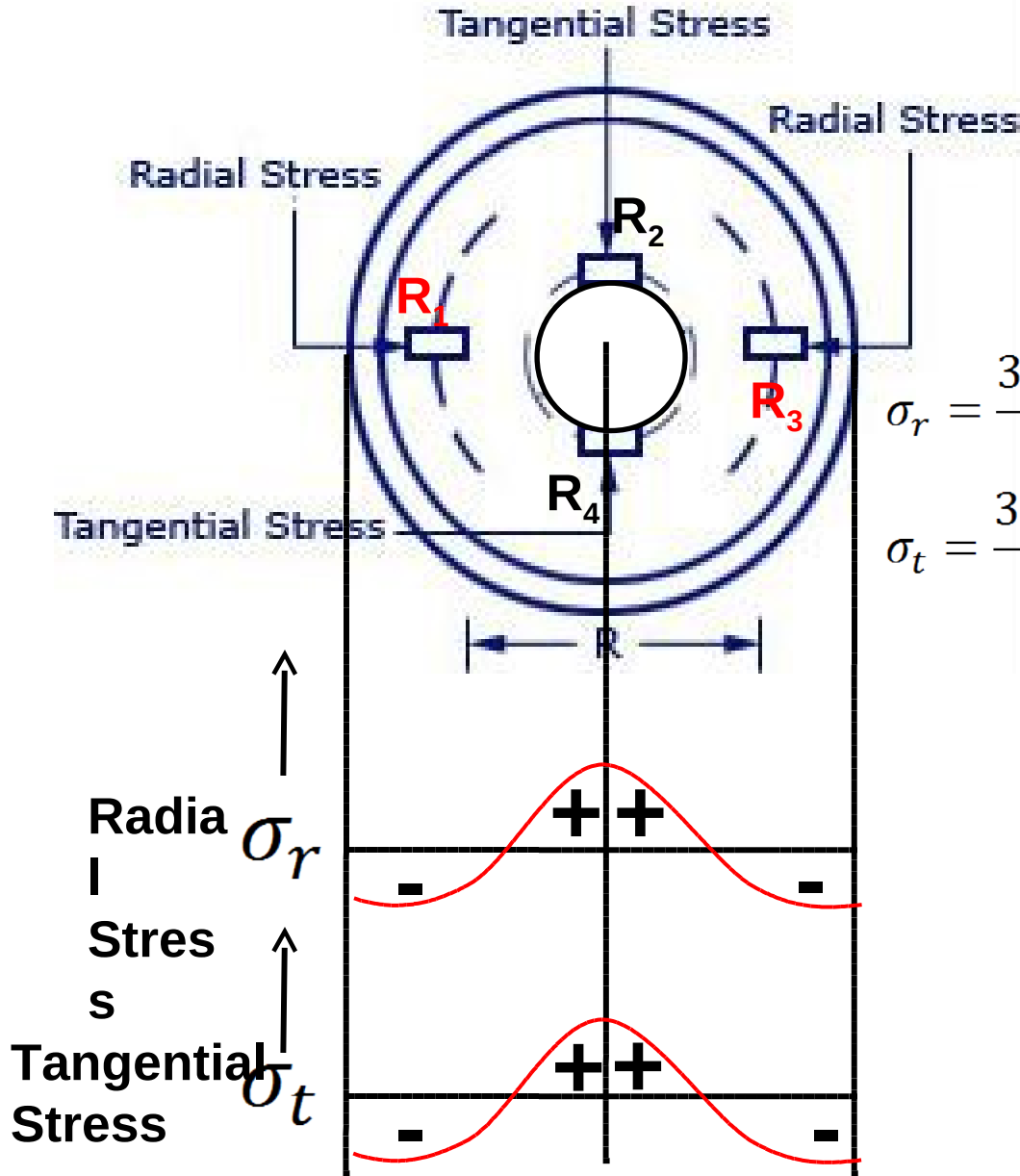
Only dynamic pressures can be measured.

# Resistance Strain-gages Pressure Transducer



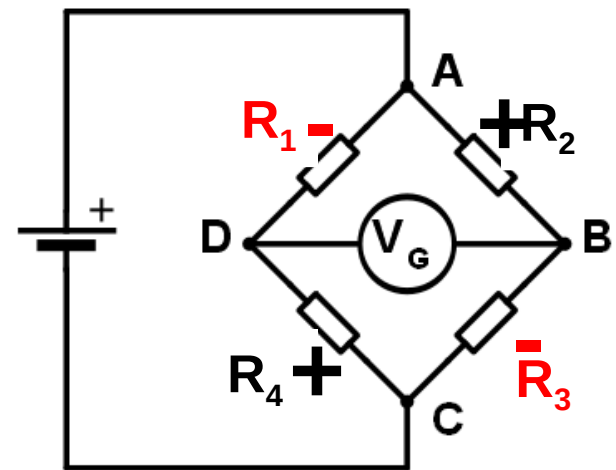
Strain gage Resistor

# Resistance Strain-gages Pressure Transducer



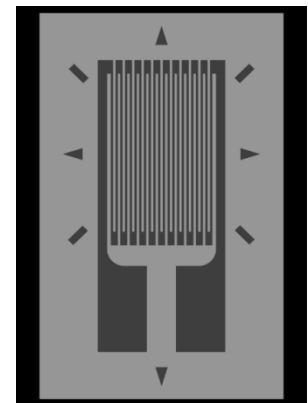
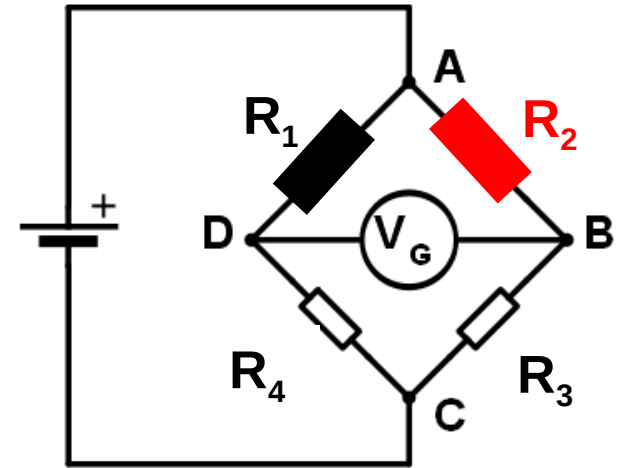
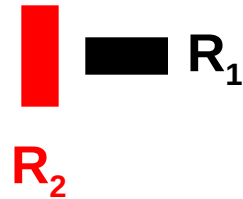
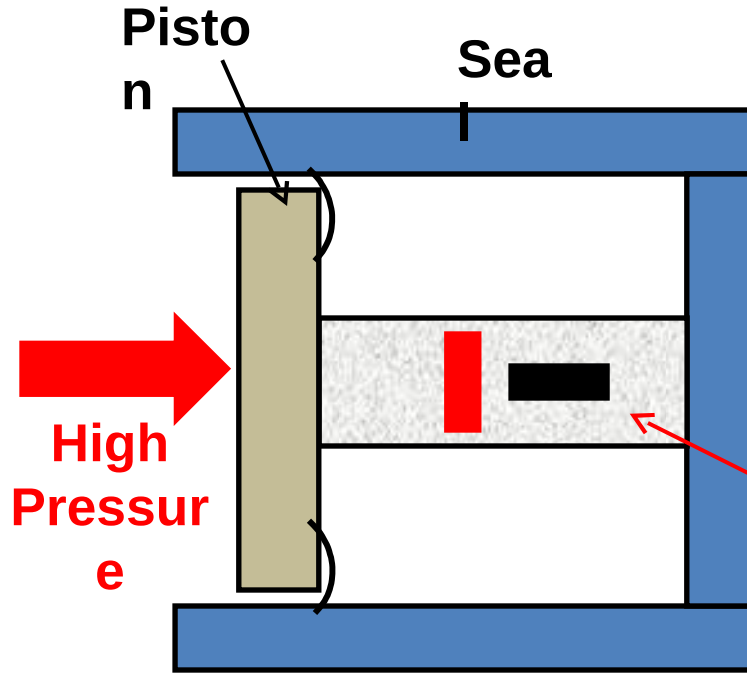
$$\sigma_r = \frac{3pR^2v}{8t^2} \left[ \left( \frac{1}{v} + 1 \right) - \left( \frac{3}{v} + 1 \right) \left( \frac{r}{R} \right)^2 \right]$$

$$\sigma_t = \frac{3pR^2v}{8t^2} \left[ \left( \frac{1}{v} + 1 \right) - \left( \frac{1}{v} + 3 \right) \left( \frac{r}{R} \right)^2 \right]$$

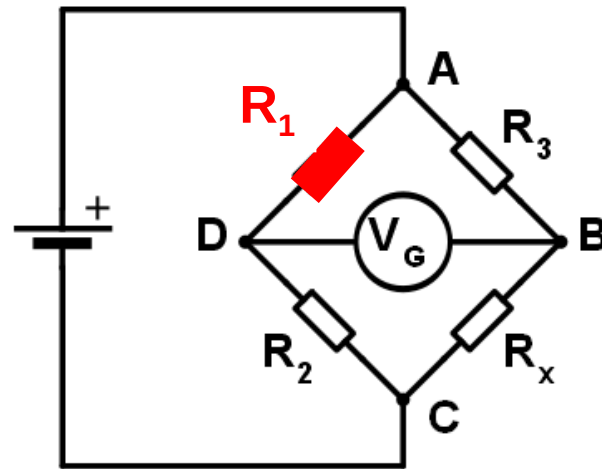
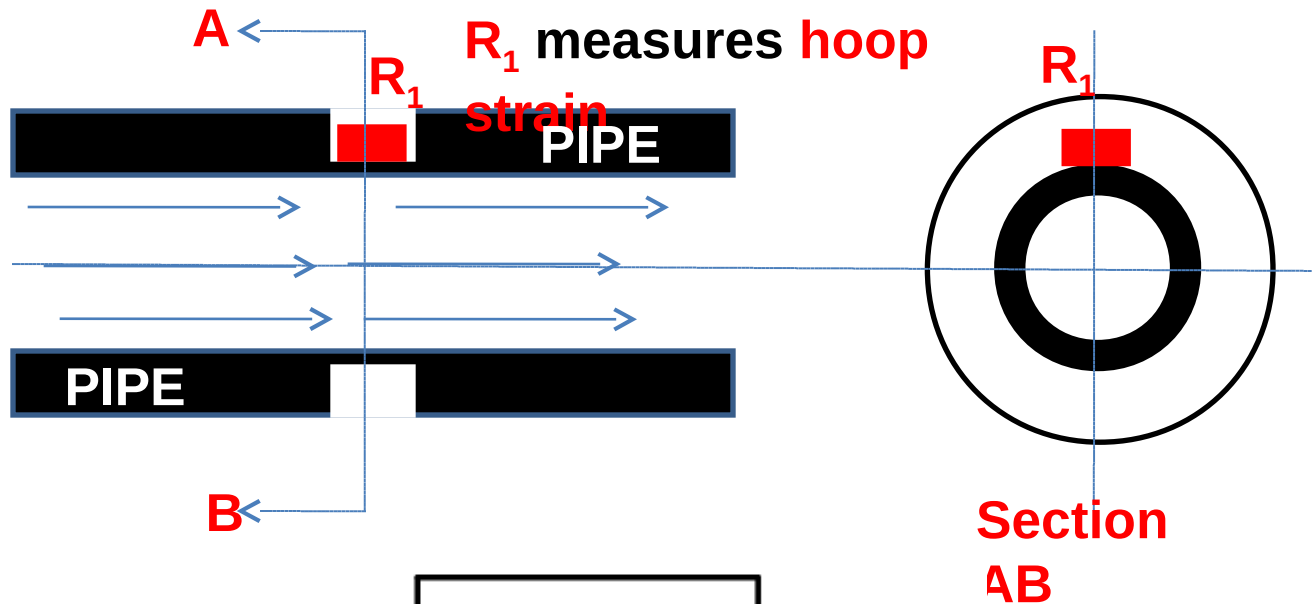


Bridge Circuit

# Piston Type Strain-gages Pressure Transducer



# Strain-gages Transducer-For Fluid Pressure



Bridge  
Circuit

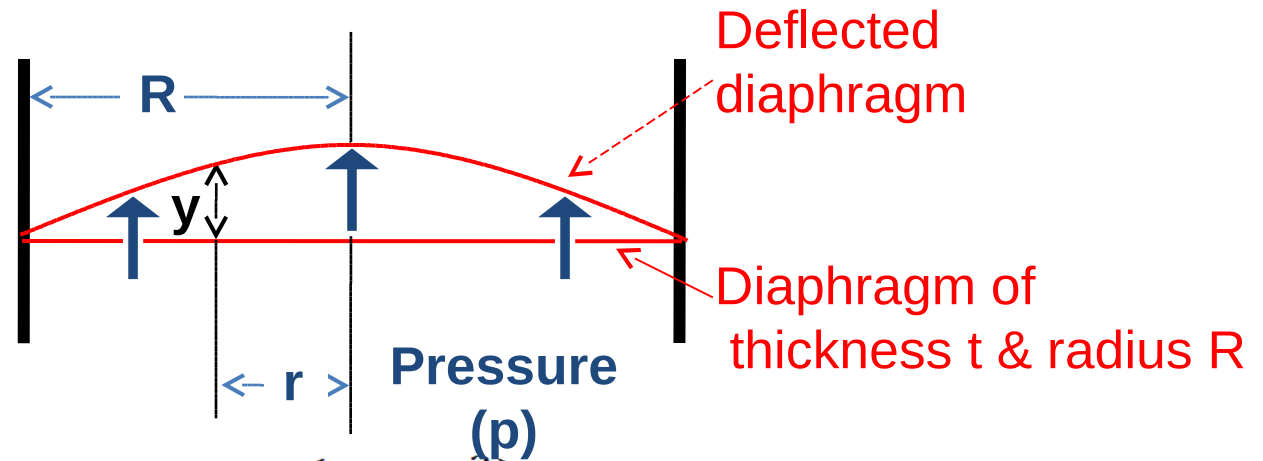
# Elastic Element Characteristics

For elastic elements used in pressure transducers

- Deflection due to pressure and
- Dynamic properties are of great importance

# Elastic Element Characteristics

## Deflection due to pressure



$$\text{Deflection at } r, \quad y = \frac{3}{16} p \frac{(1 - \nu^2)}{Et^3} (R^2 - r^2)^2$$

$p =$  pressure at  $r$ ,  $\nu =$  Poisson ratio

$t =$  thickness  $E =$  Young Modulus

$$y_{\max}(\text{at } r = 0) = \frac{3}{16} \frac{p(1 - \nu^2)}{Et^3} R^4$$

$$y_{\max} < t/3$$



# Elastic Element: Dynamic Characteristics

Fundamental frequency of vibration for a circular diaphragm of radius  $R$ , is

$$\omega_n = \frac{10.21}{R^2} \sqrt{\frac{Et^2}{12(1-\nu^2)\rho}} \text{ rad/s}$$

*Here  $\rho$  is the mass density of the diaphragm material*

*Let  $\omega_e$  be the exciting frequency of vibrations of the elastic element, then*

$$\omega_n \gg \omega_e$$

*for dynamic considerations*

# Elastic Element: Dynamic Characteristics

## “Points to consider”

The properties of pressure transmitting fluid & the connecting tubing are also important.

- The effective mass of the moving system depends on the mass of the fluid that moves with the deflected elastic diaphragm.
- The damping action depends on fluid friction.

# High Pressure Measurements